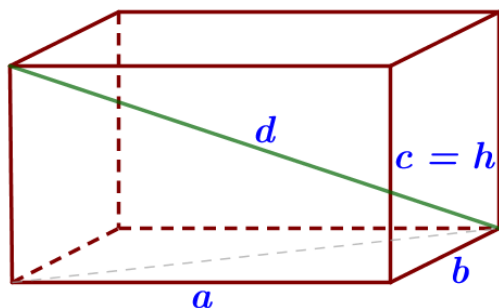


# Стереометрия

Е. А. Ширяева (www.time4math.ru)

1



$$l_{\text{реб}} = 4(a + b + c)$$

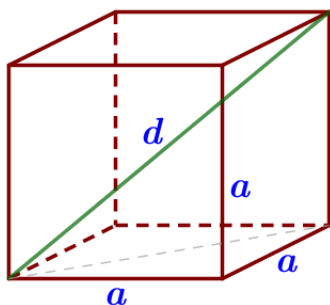
$$d^2 = a^2 + b^2 + c^2$$

$$S_{\text{бок}} = 2(S_1 + S_2) = 2(ac + bc)$$

$$S_{\text{пола}} = 2(S_1 + S_2 + S_3) = 2(ac + bc + ab)$$

$$V = abc = S_{\text{оч}} \cdot h = abh$$

2



$$l_{\text{реб}} = 12a$$

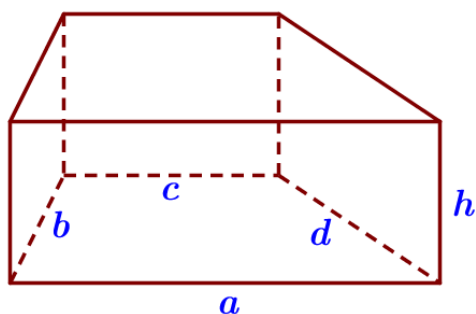
$$d = \sqrt{3}a$$

$$S_{\text{бок}} = 4a^2$$

$$S_{\text{пола}} = 6a^2$$

$$V = a^3$$

3



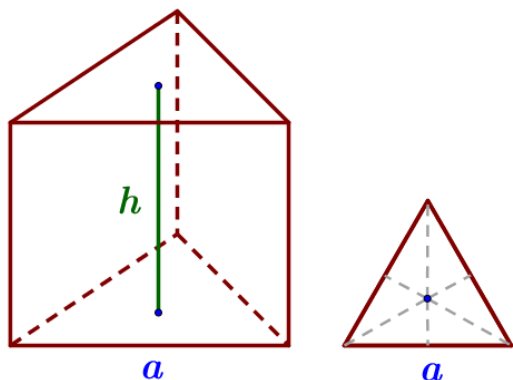
$$S_{\text{оч}} - ?$$

$$S_{\text{бок}} = P_{\text{оч}} \cdot h = (a + b + c + d) \cdot h$$

$$S_{\text{пола}} = 2S_{\text{оч}} + S_{\text{бок}}$$

$$V = S_{\text{оч}} \cdot h$$

4



$$S_{\text{оч}} = \frac{\sqrt{3}}{4} a^2$$

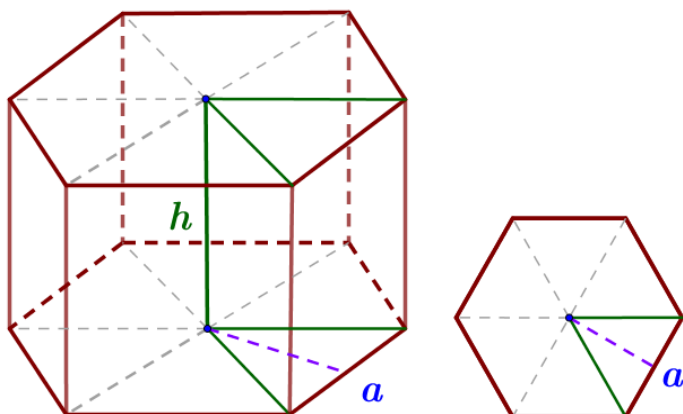
$$S_{\text{бок}} = P_{\text{оч}} \cdot h = 3ah$$

$$S_{\text{пола}} = S_{\text{бок}} + 2S_{\text{оч}}$$

$$S_{\text{пола}} = 3ah + \frac{\sqrt{3}}{2} a^2$$

$$V = S_{\text{оч}} \cdot h = \frac{\sqrt{3}}{4} a^2 h$$

5



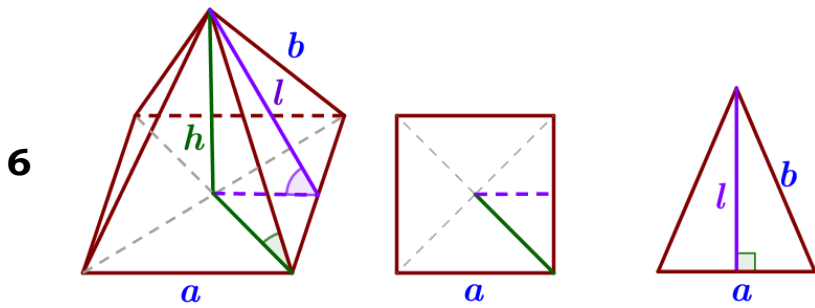
$$S_{\text{оч}} = \frac{3\sqrt{3}}{2} a^2$$

$$S_{\text{бок}} = P_{\text{оч}} \cdot h = 6ah$$

$$S_{\text{пола}} = S_{\text{бок}} + 2S_{\text{оч}}$$

$$S_{\text{пола}} = 6ah + 3\sqrt{3}a^2$$

$$V = S_{\text{оч}} \cdot h = \frac{3\sqrt{3}}{2} a^2 h$$

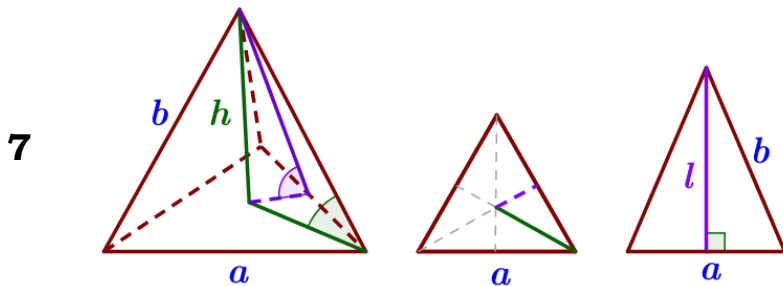


$$S_{\text{OCH}} = a^2$$

$$S_{\text{бок}} = \frac{1}{2} \cdot P_{\text{OCH}} \cdot l = 2al$$

$$S_{\text{ПОЛН}} = S_{\text{бок}} + S_{\text{OCH}} = 2al + a^2$$

$$V = \frac{1}{3} S_{\text{OCH}} \cdot h = \frac{1}{3} a^2 h$$

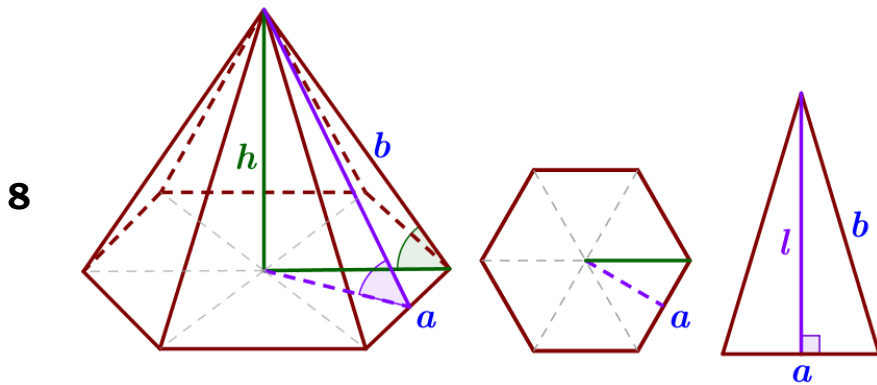


$$S_{\text{OCH}} = \frac{\sqrt{3}}{4} a^2$$

$$S_{\text{бок}} = \frac{1}{2} \cdot P_{\text{OCH}} \cdot l = 1,5al$$

$$S_{\text{ПОЛН}} = S_{\text{бок}} + S_{\text{OCH}} = 1,5al + \frac{\sqrt{3}}{4} a^2$$

$$V = \frac{1}{3} S_{\text{OCH}} \cdot h = \frac{\sqrt{3}}{12} a^2 h$$

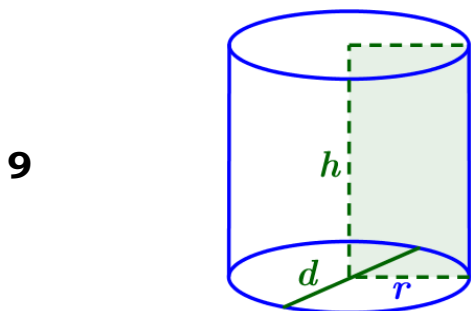


$$S_{\text{OCH}} = \frac{3\sqrt{3}}{2} a^2$$

$$S_{\text{бок}} = \frac{1}{2} \cdot P_{\text{OCH}} \cdot l = 3al$$

$$S_{\text{ПОЛН}} = S_{\text{бок}} + S_{\text{OCH}} = 3al + \frac{3\sqrt{3}}{2} a^2$$

$$V = \frac{1}{3} S_{\text{OCH}} \cdot h = \frac{\sqrt{3}}{2} a^2 h$$

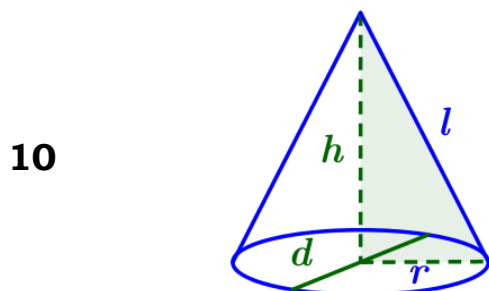


$$S_{\text{OCH}} = \pi r^2$$

$$S_{\text{бок}} = 2\pi r h$$

$$S_{\text{ПОЛН}} = S_{\text{бок}} + 2S_{\text{OCH}} = 2\pi r h + 2\pi r^2$$

$$V = S_{\text{OCH}} \cdot h = \pi r^2 h$$

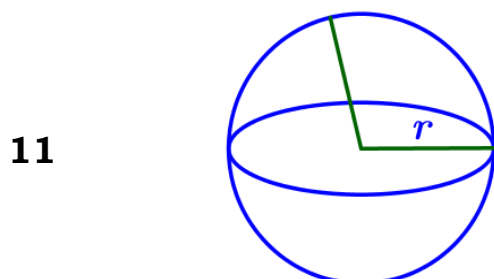


$$S_{\text{OCH}} = \pi r^2$$

$$S_{\text{бок}} = \pi r l$$

$$S_{\text{ПОЛН}} = S_{\text{бок}} + S_{\text{OCH}} = \pi r l + \pi r^2 = \pi r(l + r)$$

$$V = \frac{1}{3} S_{\text{OCH}} \cdot h = \frac{1}{3} \pi r^2 h$$



$$S_{\text{ПОВ}} = 4\pi r^2$$

$$S_{\text{сеч}} = \pi r^2$$

$$V = \frac{4}{3} \pi r^3$$